



30th Anniversary

BESIII

Measurement of hadron pair production cross sections at BESIII

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On behalf of BESIII Collaboration

Outline

➡ Motivation

➡ Data samples with BEPCII/BESIII

➡ $e^+e^- \rightarrow p\bar{p}$

- measurement of cross section
- extraction of form factors

➡ $e^+e^- \rightarrow \pi^+\pi^-\gamma$

- measurement of cross section
- extraction of form factor

➡ Summary and prospect

Data samples of BESIII

Till June, 2015

Taking data	Total Num. / Lum.	Taking time
J/ψ	225+1086 M	2009+2012
$\psi(2S)$	106+350 M	2009+2012
$\psi(3770)$	2916 pb ⁻¹	2010~2011
τ scan	24 pb ⁻¹	2011
Y(4260)/Y(4230)/Y(4360)/scan	806/1054/523/488 pb ⁻¹	2012~2013
4600/4470/4530/4575/4420	506/100/100/42/993 pb ⁻¹	2014
J/ψ line-shape scan	100 pb ⁻¹	2012
R scan (2.23, 3.40) GeV	12 pb ⁻¹	2012
R scan (3.85, 4.59) GeV	795 pb ⁻¹	2013~2014
R scan (2.0, 3.08) GeV	~525 pb ⁻¹	2014~2015

Y(2175)

~100 pb⁻¹

2015 3

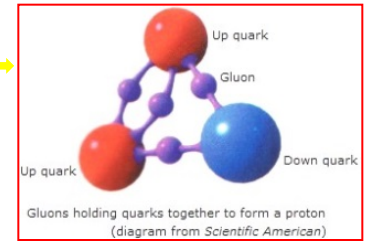


Part 1

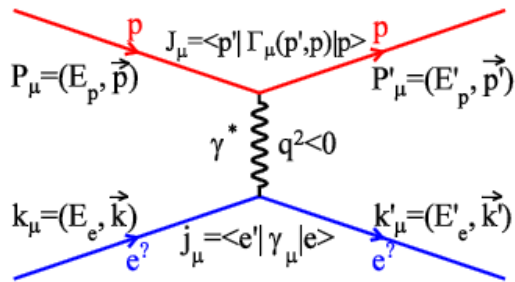
$$e^+ e^- \rightarrow p \bar{p}$$

Motivation

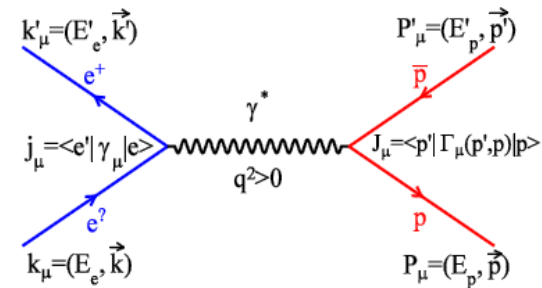
The valence-quark picture of proton in quark model:
The dynamic structure of proton can be measured in two processes:



$$e^\pm p \rightarrow e^\pm p \quad (\text{space-like } q^2 < 0)$$



$$e^+ e^- \rightarrow p \bar{p} \quad (\text{time-like } q^2 > 0)$$



BESIII

Vector current of the interaction vertex with hadronic structure

$$\Gamma_\mu(p', p) = \gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m_p} F_2(q^2)$$

Structure functions F_1 and F_2 can be recombined into two form factors

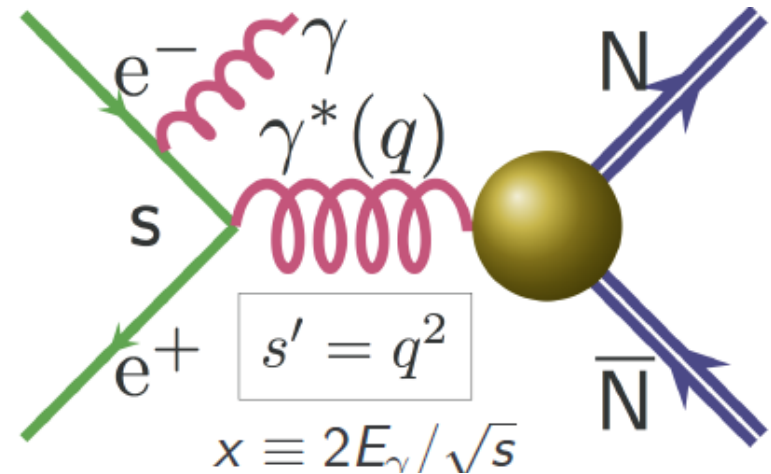
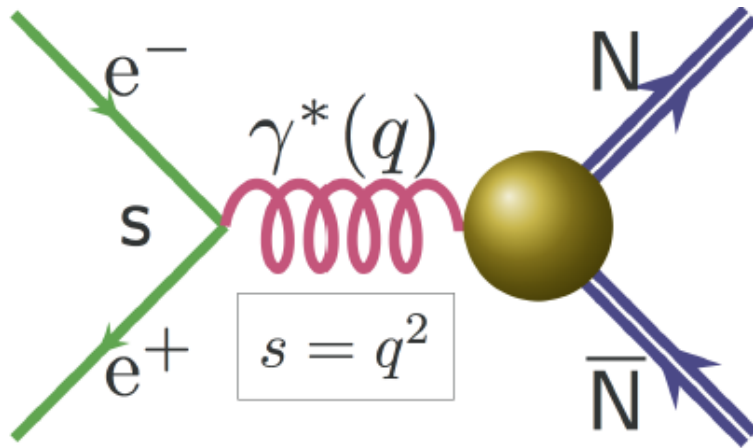
- **Electronic:** $G_E(q^2) = F_1(q^2) + \tau \kappa_p F_2(q^2)$
 - **Magnetic:** $G_M(q^2) = F_1(q^2) + \kappa_p F_2(q^2)$
- $\tau = \frac{q^2}{4m_p^2}, \quad \kappa_p = \frac{g_p - 2}{2} = \mu_p - 1$

More directly perceived through the senses, G_E and G_M relate to the spatial distribution of charge and magnetization in Breit frame, e.g, the charge density distribution.

$$\rho(\vec{r}) = \int \frac{d^3q}{2\pi^3} e^{-i\vec{q}\cdot\vec{r}} \frac{M}{E(\vec{q})} G_E(\vec{q}^2)$$

Two methods

For time-like process



	Energy Scan	Initial State Radiation
E_{beam}	discrete	fixed
\mathcal{L}	low at each beam energy	high at one beam energy
σ	$\frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\alpha^2 \beta C}{4q^2} [G_M ^2 (1 + \cos^2\theta) + \frac{4m_p^2}{q^2} G_E ^2 \sin^2\theta]$	$\frac{d^2\sigma_{p\bar{p}\gamma}}{dx d\theta_\gamma} = W(s, x, \theta_\gamma) \sigma_{p\bar{p}}(q^2)$ $W(s, x, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2 - 2x + x^2}{\sin^2\theta_\gamma} - \frac{x^2}{2} \right)$
q^2	single at each beam energy	from threshold to s

This talk

In progress

Cross section

For the process $e^+e^- \rightarrow p\bar{p}$, differential cross section

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2\beta}{4s} C[|G_M(s)|^2(1 + \cos^2\theta) + \frac{1}{\tau}|G_E(s)|^2\sin^2\theta]$$

$$\beta = \sqrt{1 - 4M^2/s}$$

$$\tau = s/4M^2,$$

$$y = \pi\alpha M/\beta\sqrt{s}$$

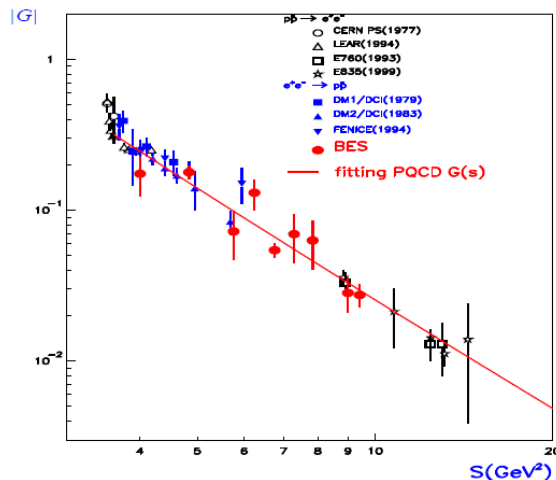
the Born cross section

$$\sigma = \frac{4\alpha^2\pi\beta}{3s} C[|G_M(s)|^2 + \frac{1}{2\tau}|G_E(s)|^2]$$

Coulomb correction C is subtle and important near threshold ($\beta \rightarrow 0$).

$$C = \frac{y}{1 - \exp(-y)}$$

Due to the limited statistics, early experiments assume $|G_E| = |G_M| \equiv |G|$



BES Collaboration, Phys. Lett. B630, (2005)14

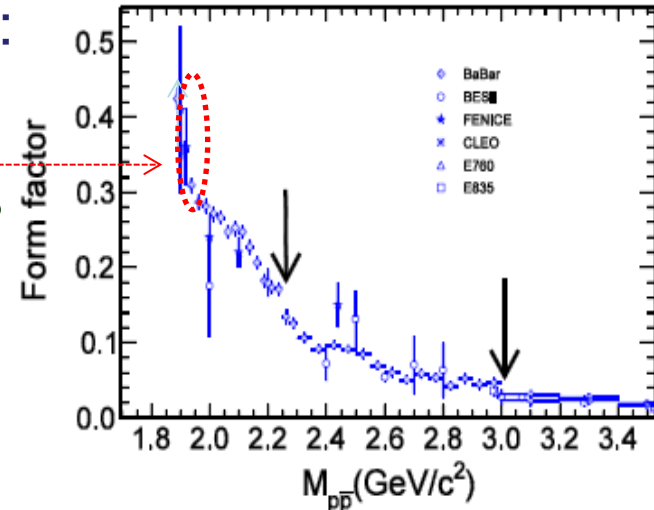
BESII measured $|G|$ and parameterized as (Λ :QCD scale, A : free parameter)

$$|G(s)| = \frac{A}{s^2 \ln^2(s/\Lambda^2)}$$

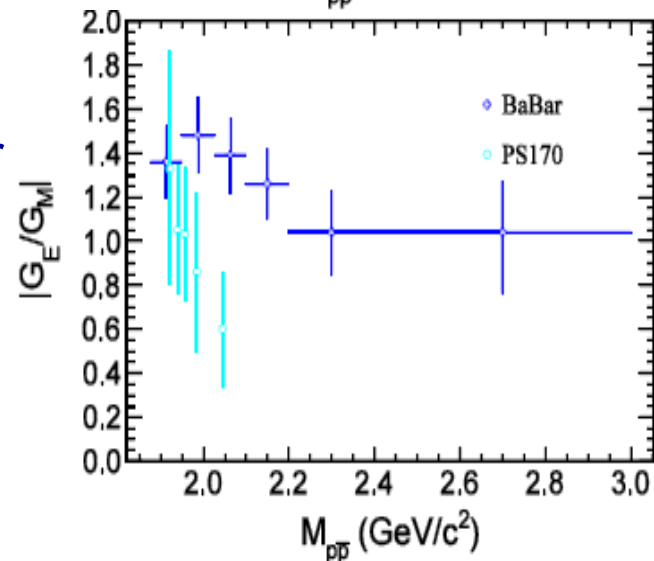
Some question to make clear

Recent years, statistics of data samples increased, the behavior of form factor seems clear, but some questions still left:

- Steep rise toward threshold ?
 - Two rapid decreases around 2.25 and 3.0 GeV ?
- Are they true?



- Ratio $|G_E/G_M|$ disagreement by PS170 and BaBar
 - Poor precision ($\sim 11\%$, 43%)
 - Limited energy range
- which one is reliable?

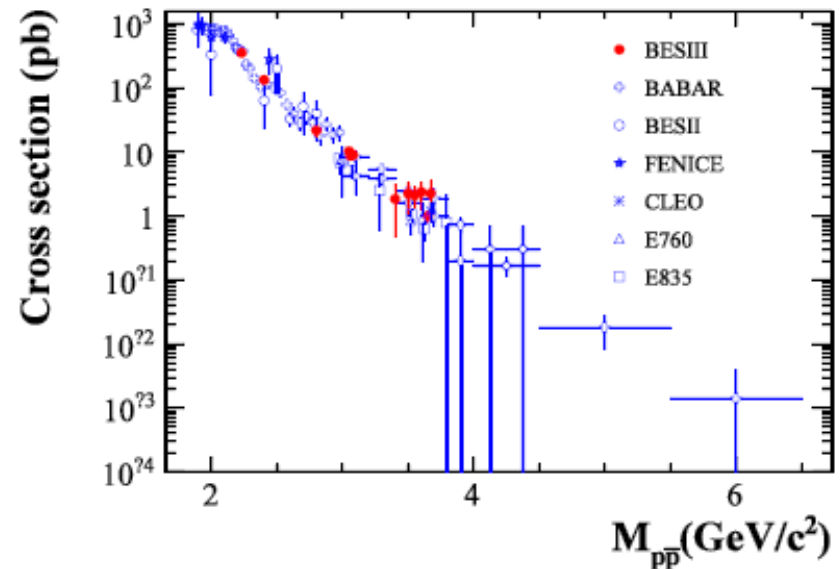
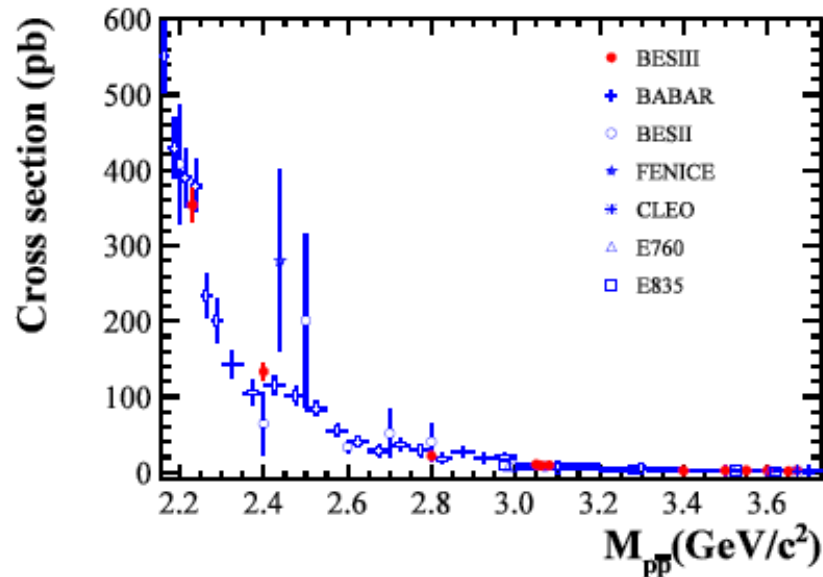


Measurement of cross section

Experimental formula for cross section:

$$\sigma_{\text{Born}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{L \cdot \epsilon \cdot (1 + \delta)}$$

- N_{obs} : the observed number of signal in data
- N_{bkg} : the number of background evaluated from MC
- L : the integral luminosity
- ϵ : detection efficiency by MC sample, with Conexc generator
- $(1 + \delta)$: radiative correction factor



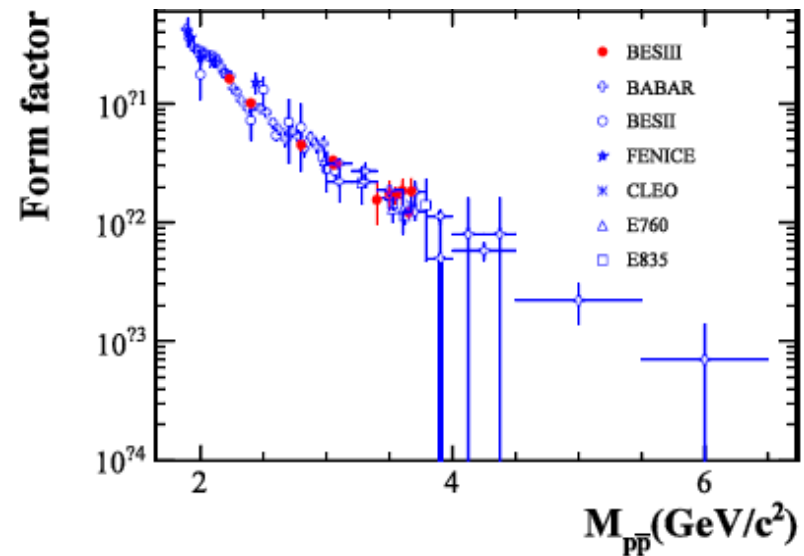
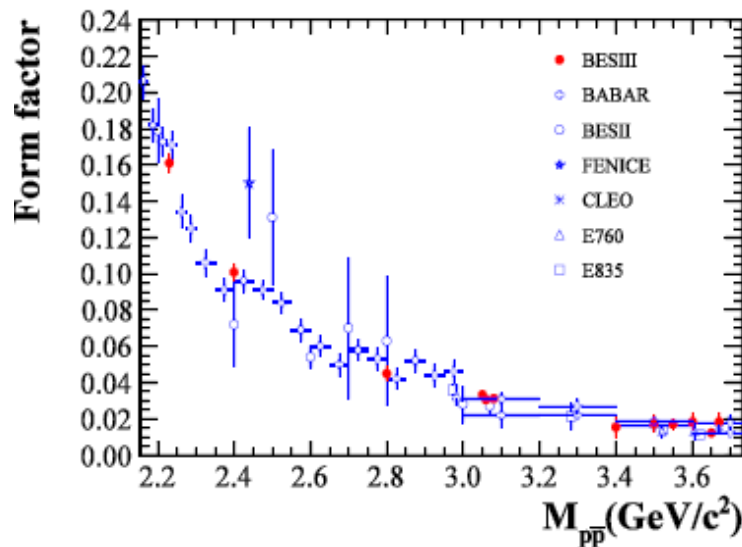
Extraction of effective form factor

In order to compare with earlier measurements, we still assume $|G_E|=|G_M|\equiv|G_{eff}|$, and the cross section reads

$$\sigma = \frac{\pi\alpha^2}{3m_p^2\tau} \left[1 + \frac{1}{2\tau} \right] |G_{eff}|^2$$

Then the effective form factor could be extracted

$$G_{eff} = \sqrt{\frac{\sigma_{Born}}{86.83 \cdot \frac{\beta}{s} \left(1 + \frac{2m_p^2}{s} \right)}}$$



The result with BESIII data are consistent with other measurements within errors.

Extraction of electromagnetic $|G_E/G_M|$ ratio

- Angular distribution:

$$\frac{d\sigma}{d\Omega}(q^2) = \frac{\alpha^2 \beta}{4s} |G_M(s)|^2 \left[(1 + \cos^2 \theta_p) + R_{\text{em}}^2 \frac{1}{\tau} \sin^2 \theta_p \right]$$

- $R_{\text{em}} = G_E(q^2)/G_M(q^2)$
- θ_p : polar angle of proton

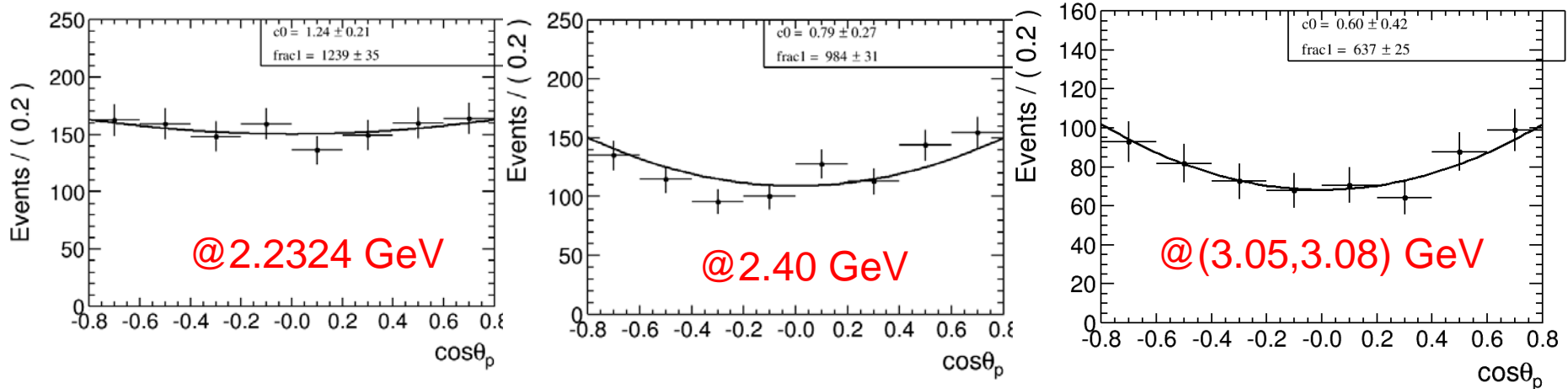
- Fit function:

$$\frac{dN}{d\cos\theta_p} = N_{\text{norm}} \left[(1 + \cos^2 \theta_p) + R_{\text{em}}^2 \frac{1}{\tau} \sin^2 \theta_p \right]$$

the overall normalization

$$N_{\text{norm}} = \frac{2\pi\alpha^2\beta L}{4s} \left[1.94 + 5.04 \frac{m_p^2}{s} R^2 \right] G_M(s)^2$$

- Results:



Extraction of electromagnetic $|G_E/G_M|$ ratio

- Method of moment:

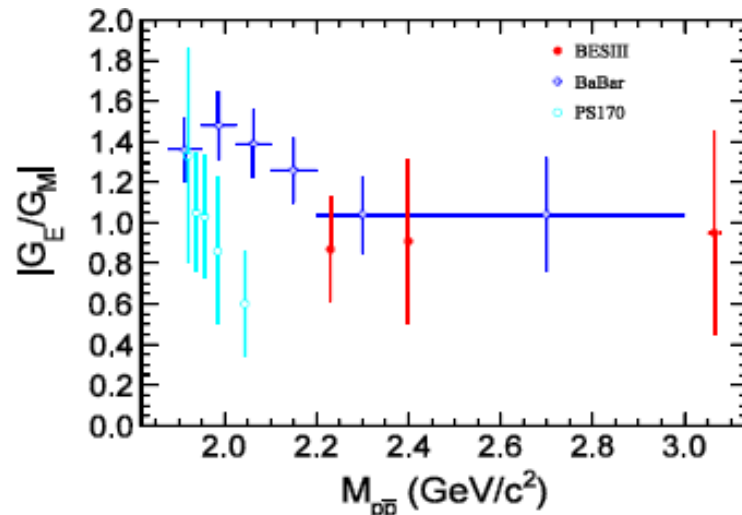
- second moment of $\cos\theta_p$: $\langle \cos^2\theta_p \rangle = \frac{1}{N_{\text{norm}}} \int \cos^2\theta_p \frac{d\sigma}{d\Omega} d\cos\theta_p$

- Estimator of $\cos\theta_p$: $\langle \cos^2\theta_p \rangle = \overline{\cos^2\theta_p} = \frac{1}{N} \sum_{i=1}^N \cos^2\theta_{p,i} / \epsilon_i$

- Extraction of $|G_E/G_M| = R = \sqrt{\frac{s}{4m_p^2} \frac{\langle \cos^2\theta_p \rangle - 0.243}{0.108 - 0.648 \langle \cos^2\theta_p \rangle}}$

- Uncertainty: $\langle \cos^2\theta_p \rangle: \sigma_{\langle \cos^2\theta_p \rangle} = \sqrt{\frac{1}{N-1} [\langle \cos^4\theta_p \rangle - \langle \cos^2\theta_p \rangle^2]}$

- Result:



Result measured with BESIII is consistent with BaBar's, but not with PS170.

Extraction of electromagnetic ratio $|G_E/G_M|$

\sqrt{s} (MeV)	$ G_E/G_M $	$ G_M $ ($\times 10^{-2}$)	χ^2/ndf
Fit on $\cos \theta_p$			
2232.4	$0.87 \pm 0.24 \pm 0.05$	$18.42 \pm 5.09 \pm 0.98$	1.04
2400.0	$0.91 \pm 0.38 \pm 0.12$	$11.30 \pm 4.73 \pm 1.53$	0.74
(3050.0, 3080.0)	$0.95 \pm 0.45 \pm 0.21$	$3.61 \pm 1.71 \pm 0.82$	0.61
<i>method of moment</i>			
2232.4	0.83 ± 0.24	18.60 ± 5.38	-
2400.0	0.85 ± 0.37	11.52 ± 5.01	-
(3050.0, 3080.0)	0.88 ± 0.46	3.34 ± 1.72	-

Phys. Rev. D 91, 112004. (June 9, 2015)



Part 2

$$e^+ e^- \rightarrow \pi^+ \pi^- \gamma$$

Motivation

The Dirac equation of a charged fermion in electromagnetic field (\vec{A}, \vec{B})

$$i\hbar \frac{\partial}{\partial t} \varphi = \left[\frac{1}{2m} \left(\vec{P} + \frac{e}{c} \vec{A} \right)^2 + \frac{e\hbar}{2mc} \vec{\sigma} \cdot \vec{B} - e\phi \right] \varphi$$

point-like fermion has magnetic moment

$$\vec{\mu} = -\frac{e\hbar}{2mc} \vec{\sigma} = -\frac{e}{mc} \vec{S}$$

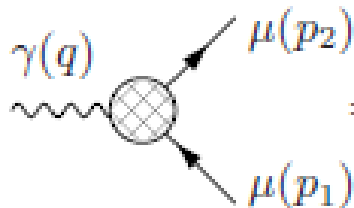
define Bohr magneton:

$$\mu_B = \frac{e\hbar}{2mc}$$

the magnetic moment of bare fermion:

$$\mu = g\mu_B S \quad g = 2$$

Considering the radiative correction of the vertex



$\Rightarrow g \neq 2 \Rightarrow$ anomalous magnetic moment: $a_\mu = (g_\mu - 2)/2$

Motivation

The Standard Model (SM) prediction for muon ($g-2$):

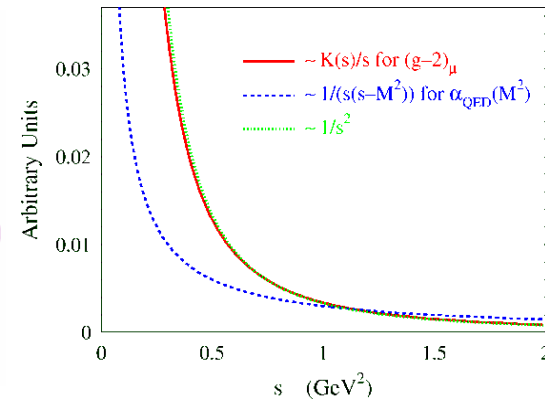
$$\begin{aligned}
 a_{\mu}^{\text{SM}} &= a_{\mu}^{\text{QED}} + a_{\mu}^{\text{had,LO}} + a_{\mu}^{\text{had,HO}} + a_{\mu}^{\text{had,LBL}} + a_{\mu}^{\text{weak}} \\
 &= \text{[Feynman diagrams]} \\
 &= (\text{QED}) \quad (11\,658\,470.35 \pm 0.28) 10^{-10} \text{ (5-loop!)} \\
 &\quad + (\text{had,LO}) \quad (684.7 \text{ to } 709.0 \pm 6) 10^{-10} \text{ (Big spread, largest error)} \\
 &\quad + (\text{had,HO}) \quad (-10.0 \pm 0.6) 10^{-10} \\
 &\quad + (\text{had,LBL}) \quad (8.0 \pm 4.0) 10^{-10} \text{ (sign change since 1998)} \\
 &\quad + (\text{weak}) \quad (15.4 \pm 0.2) 10^{-10} \text{ (2-loop)}
 \end{aligned}$$

$a_{\mu}^{\text{had,LO}}$ from data via dispersion integral

$$a_{\mu}^{\text{had,LO}} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} \sigma_{\text{had}}^0(s) K(s) ds$$

Recent data included CMD-2,
SND, BES 2-5 GeV, ALEPH τ .
NEW: CMD-2 prelim update

σ_{had}^0 bare cross-section for $e^+e^- \rightarrow \text{hadrons}$, i.e. taking out radiative corrections.
QED kernel $K(s) \sim m_{\mu}^2/3s$, gives strong weight to low energy data.



Motivation

Discrepancy between SM and experiments:

$$a_\mu^{\text{EXP}} = 116592089 (63) \times 10^{-11}$$

E821 – Final Report: PRD73 (2006) 072
with latest value of $\lambda = \mu_b/\mu_p$ (Codata '06)

$a_\mu^{\text{SM}} \times 10^{11}$	$(\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}}) \times 10^{11}$	σ
[1] 116 591 773 (53)	316 (82)	3.8
[2] 116 591 782 (59)	307 (86)	3.6
[3] 116 591 834 (49)	255 (80)	3.2
[4] 116 591 773 (48)	316 (79)	4.0
[5] 116 591 929 (52)	160 (82)	2.0

[1] HMNT06, PLB649 (2007) 173.

[2] F. Jegerlehner and A. Nyffeler, arXiv:0902.3360.

[3] Davier et al, arXiv:0908.4300 August 2009 (includes BaBar)

[4] Hagiwara, Liao, Martin, Nomura, Teubner, Oct '09 (preliminary)

[5] Davier et al, arXiv:0906.5443v2 August 2009 (τ data).

with $a_\mu^{\text{HHO}}(|b|) = 105 (26) \times 10^{-11}$

Motivation

Ratio of the contribution of theoretical uncertainty of $(g-2)$ from the measured hadronic cross section in different energy region:

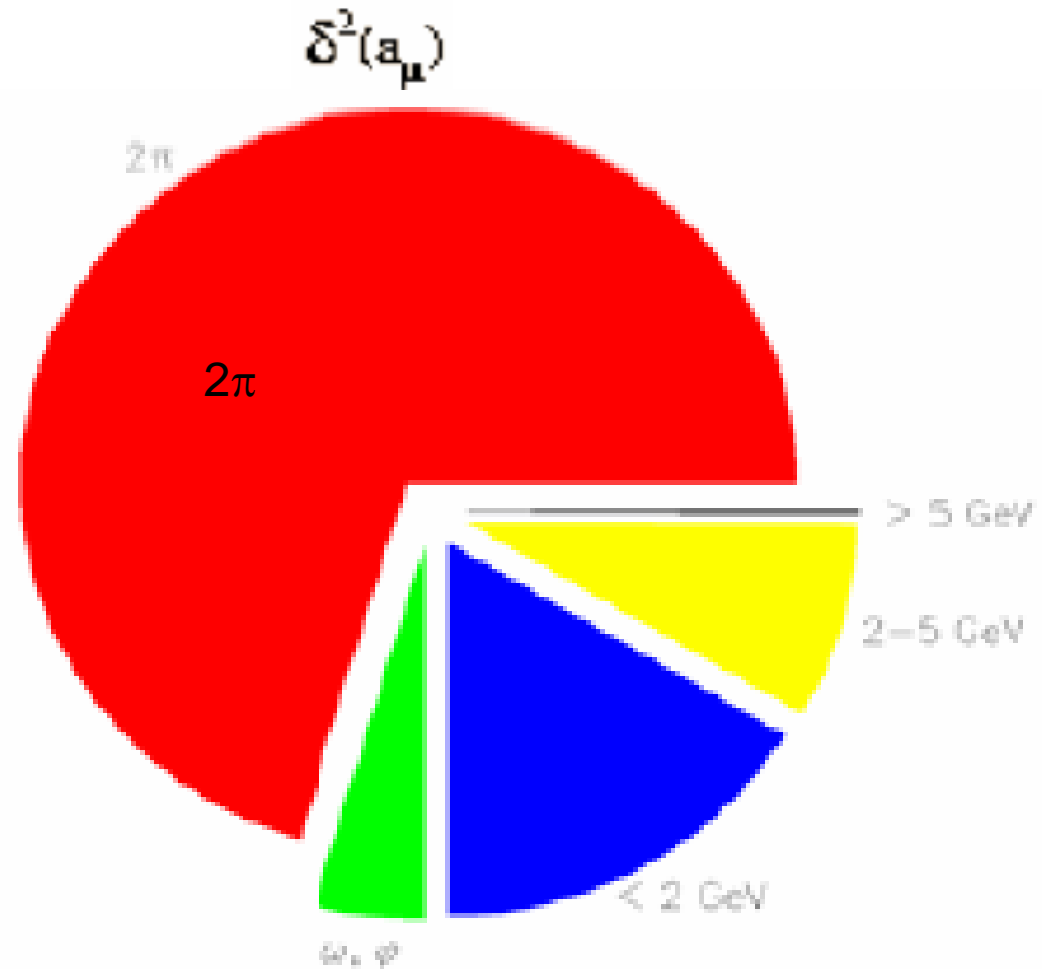
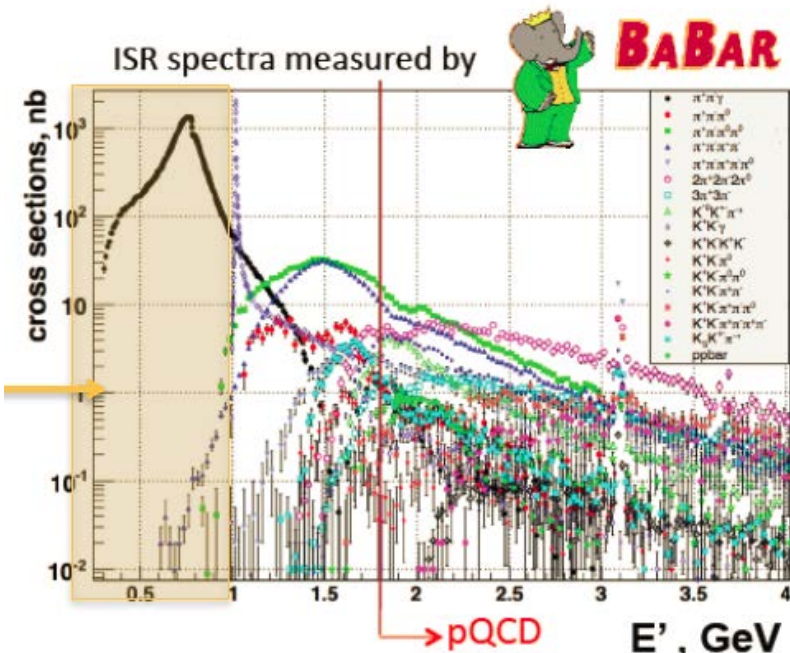
$a_\mu^{\text{had,LO}}$ from data via dispersion integral

$$a_\mu^{\text{had,LO}} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} \sigma_{\text{had}}^0(s) K(s) ds$$

$$K(s) \propto 1/s \quad \sigma(s) \propto 1/s$$

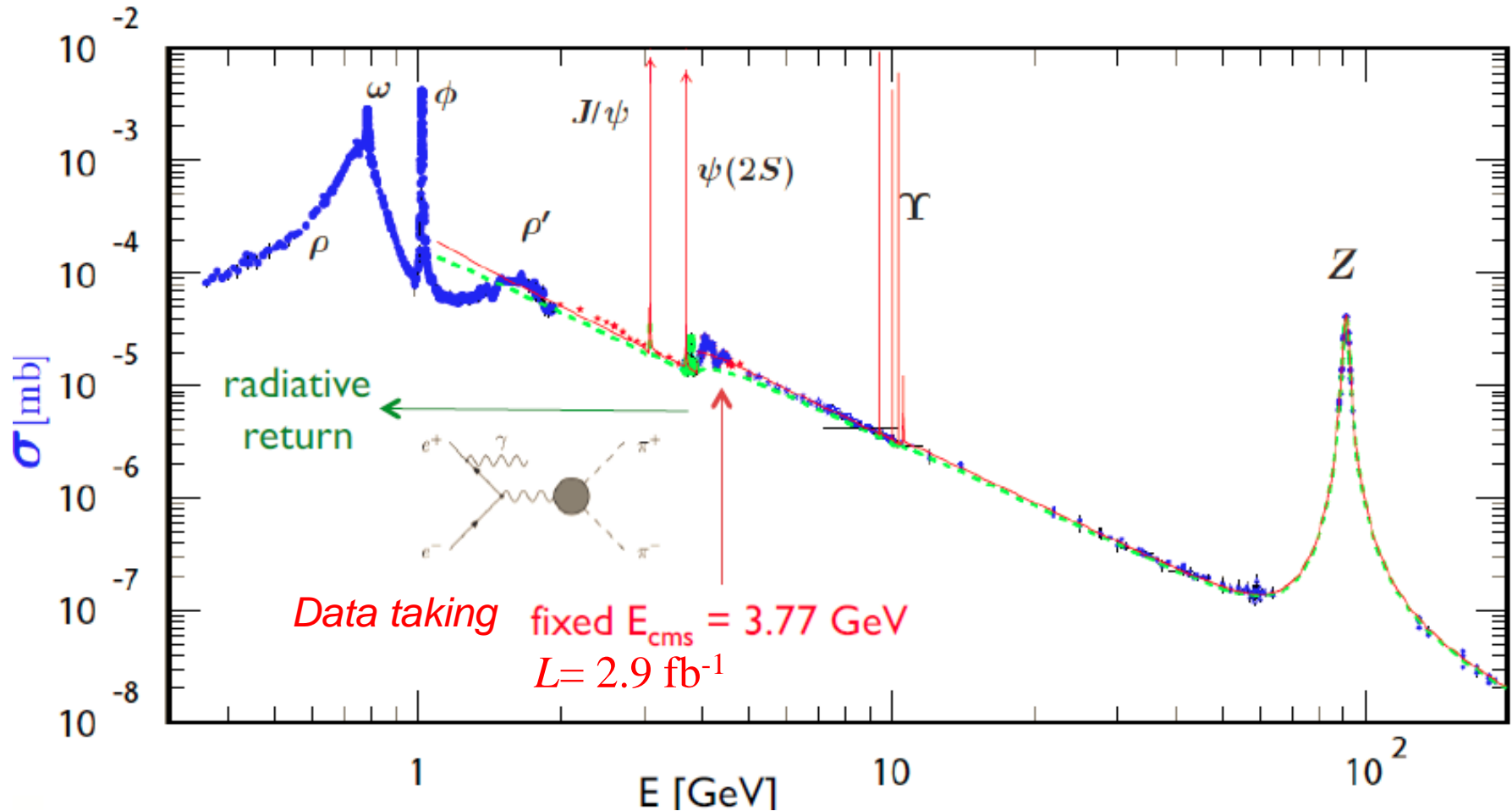
The largest contribution is below 1 GeV.

Channel $e^+e^- \rightarrow \pi^+\pi^-$ is the most important one



Initial state radiation

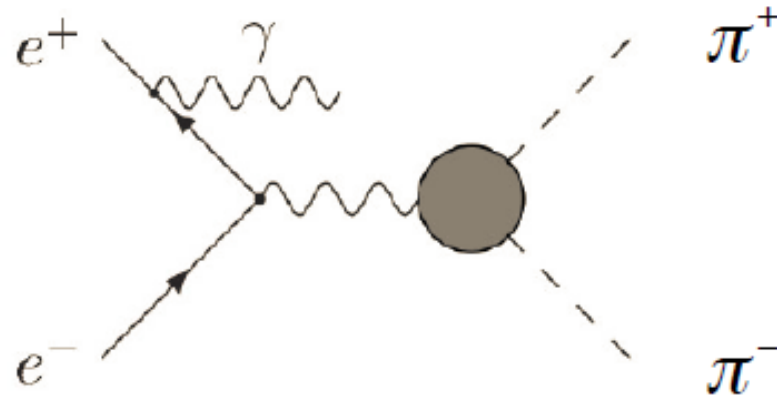
In the e^\pm collider, photon emitted from initial e^\pm decrease the effective $s' = s(1 - E_\gamma/E)$ continuously, this makes measurement at lower different energies possible.



Initial state radiation (ISR return)

Study the channel

$$e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$$



to measure the cross section of $e^+e^- \rightarrow \pi^+\pi^-$
via

$$\frac{d\sigma_{ISR}(M_{2\pi})}{dM_{2\pi}} = \frac{2M_{2\pi}}{s} W(s, x, \theta_\gamma) \cdot \sigma(M_{2\pi})$$

(neglecting FSR)

invariant mass of 2π

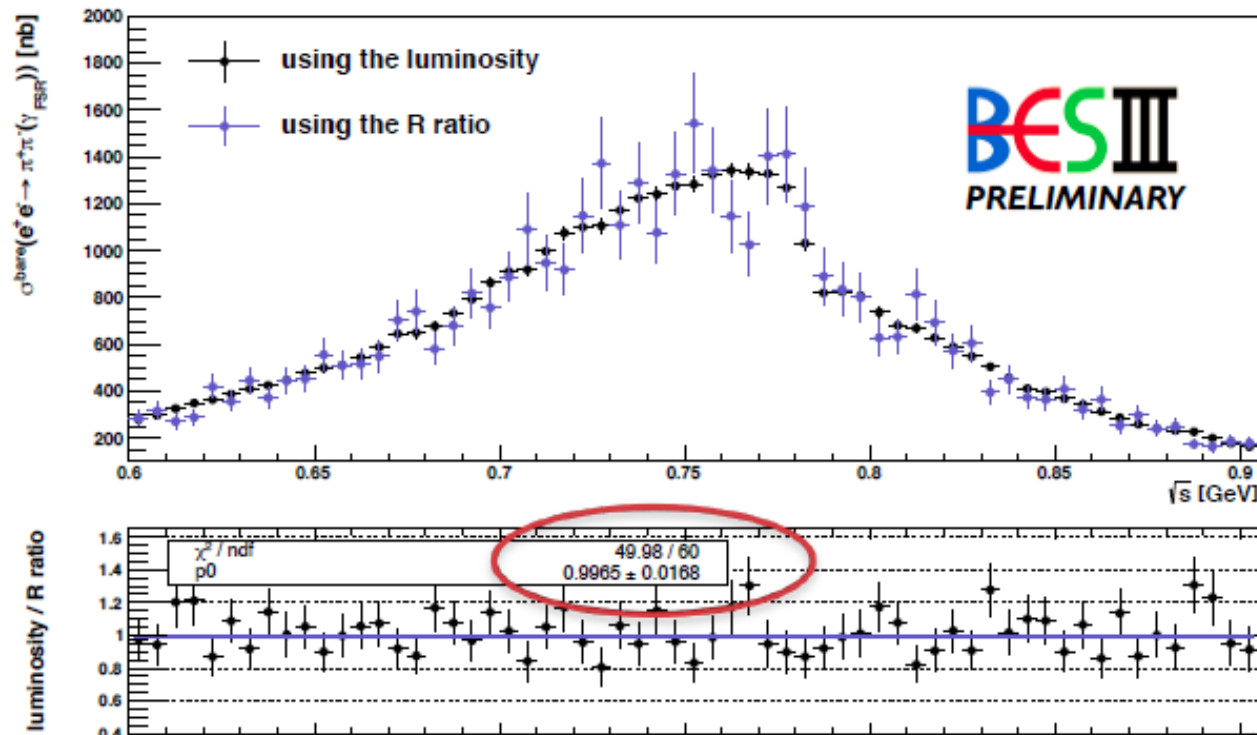
Radiator function

Two normalization methods

- Normalization to integrated luminosity

$$\sigma^{bare}(e^+e^- \rightarrow \pi^+\pi^-(\gamma_{FSR})) = \frac{N_{\pi\pi\gamma} / \varepsilon}{L_{int} \cdot H_{rad} \cdot \delta_{vac} \cdot (1 + \delta_{FSR})}$$

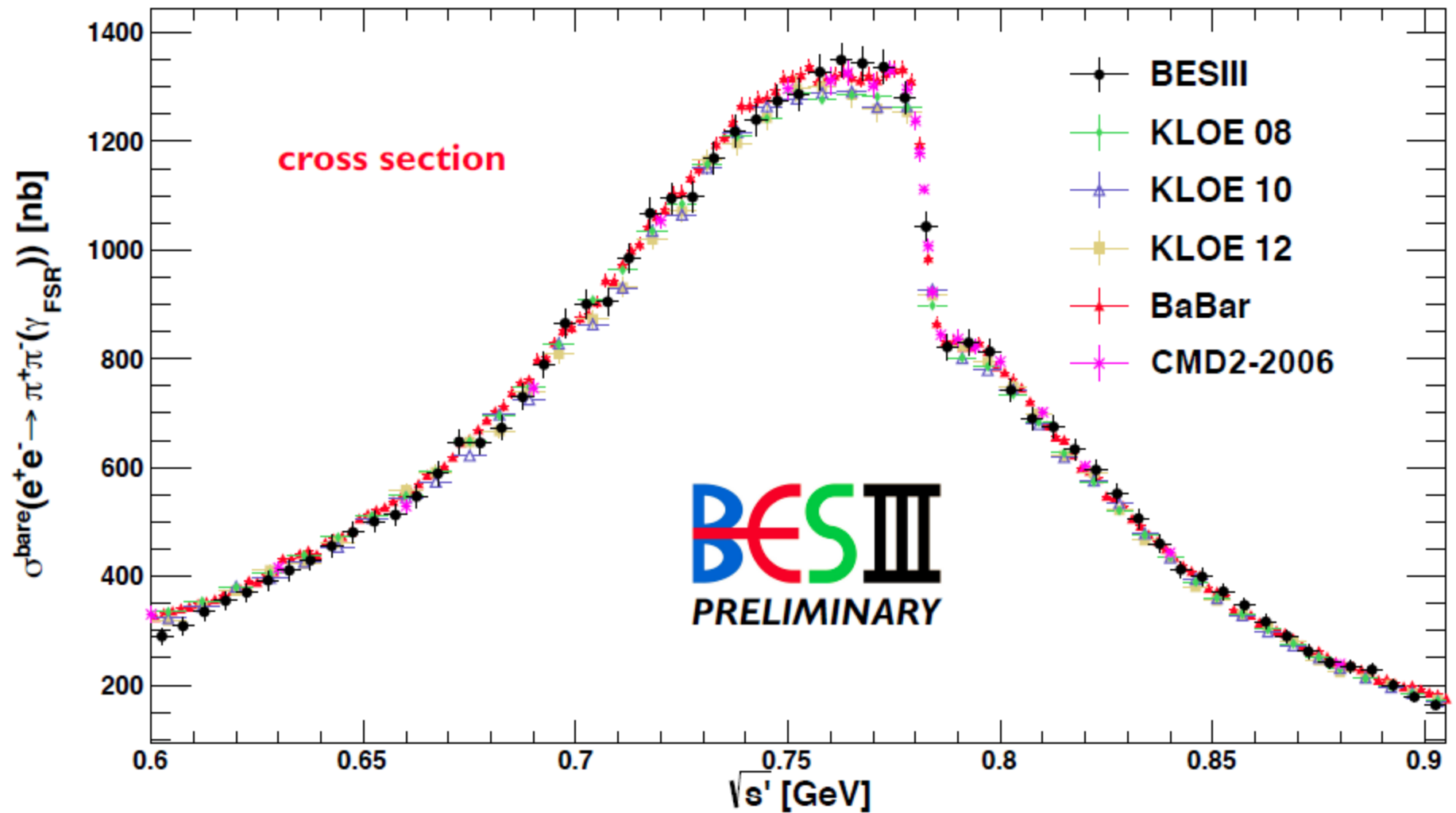
- Normalization to $\mu^+\mu^- \gamma$ events, i.e. R ratio $\pi^+\pi^- \gamma / \mu^+\mu^- \gamma$
 $\longrightarrow L_{int}, H_{rad}, \delta_{vac}$ canceled



Luminosity / R ratio – 1
 = $(0.35 \pm 1.68) \%$

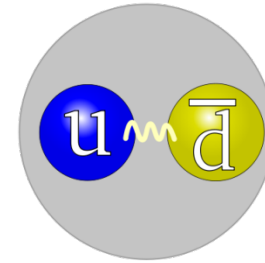
limited by $\mu^+\mu^- \gamma$ statistics

Cross section



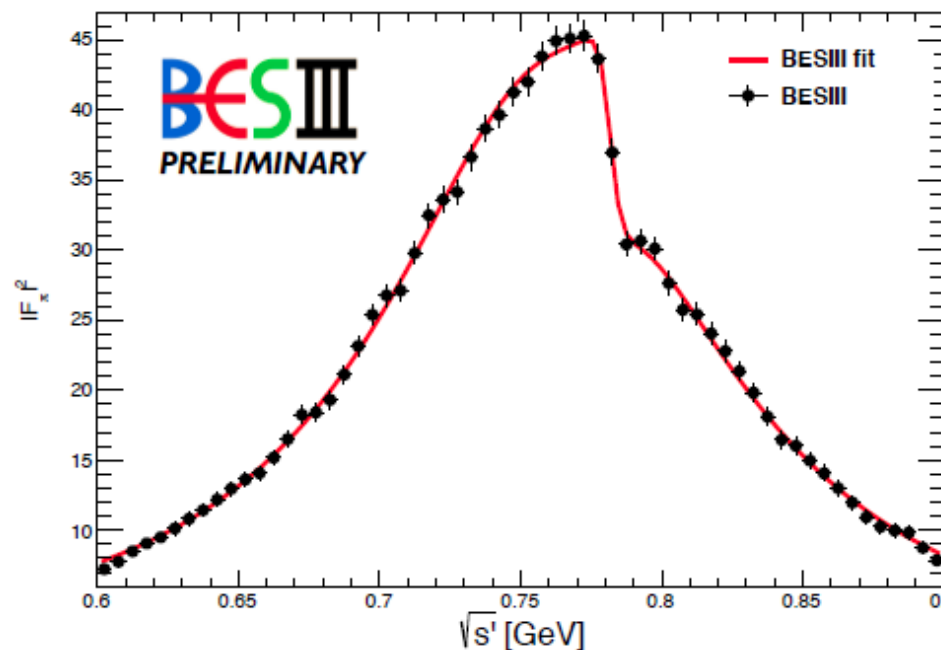
Extraction of form factor

The picture of pion structure in quark model:

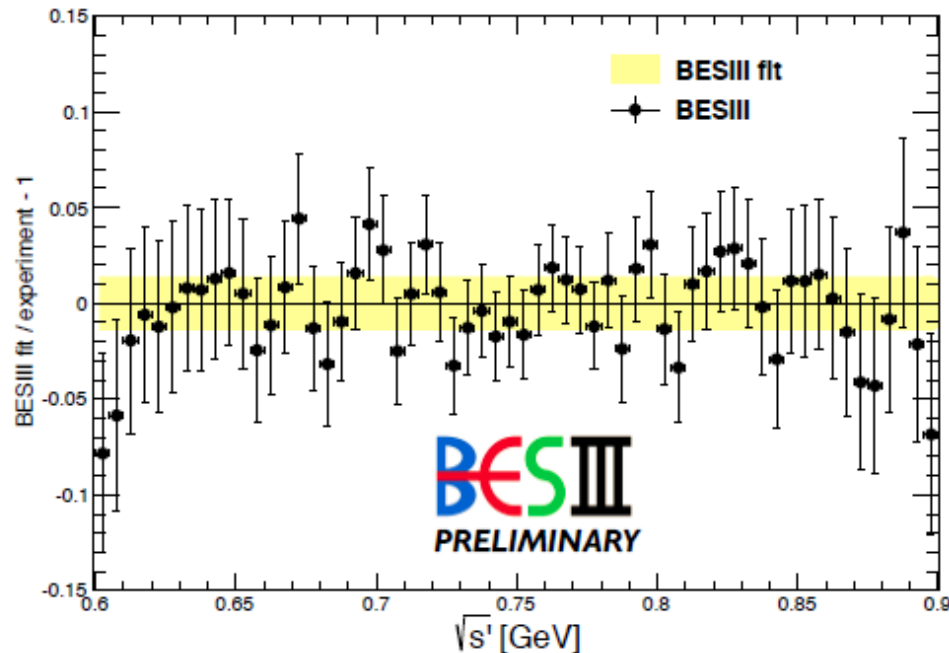


Not a point-like particle \Rightarrow pion form factor

$$|F_\pi|^2(s') = \frac{3s'}{\pi\alpha\beta_\pi^3(s')} \sigma(e^+e^- \rightarrow \pi^+\pi^-)(s') \quad , \quad \beta_\pi(s') = \sqrt{1 - \frac{4m_\pi^2}{s'}}$$

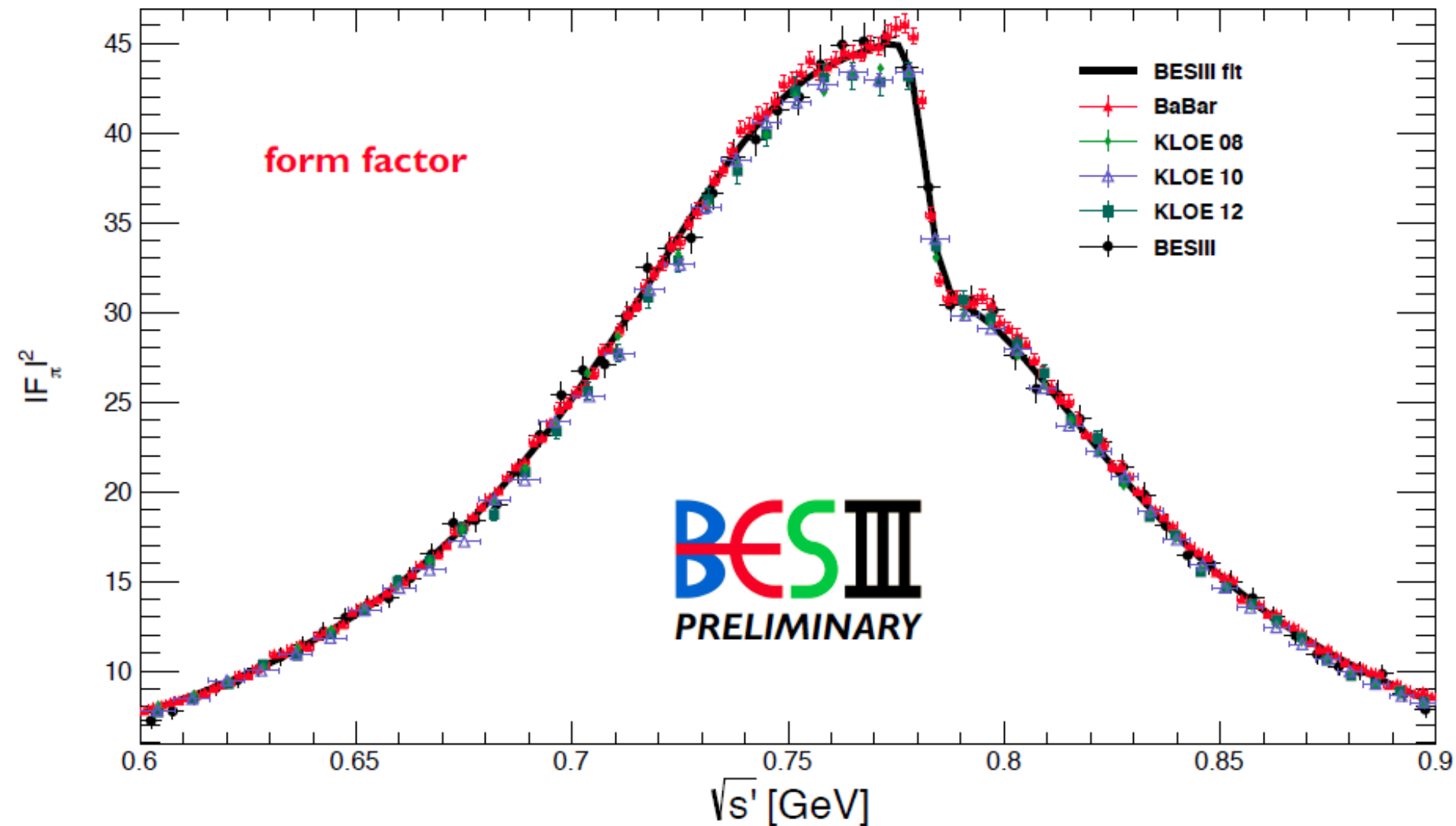


Fit function: Gounaris-Sakurai Parameterization

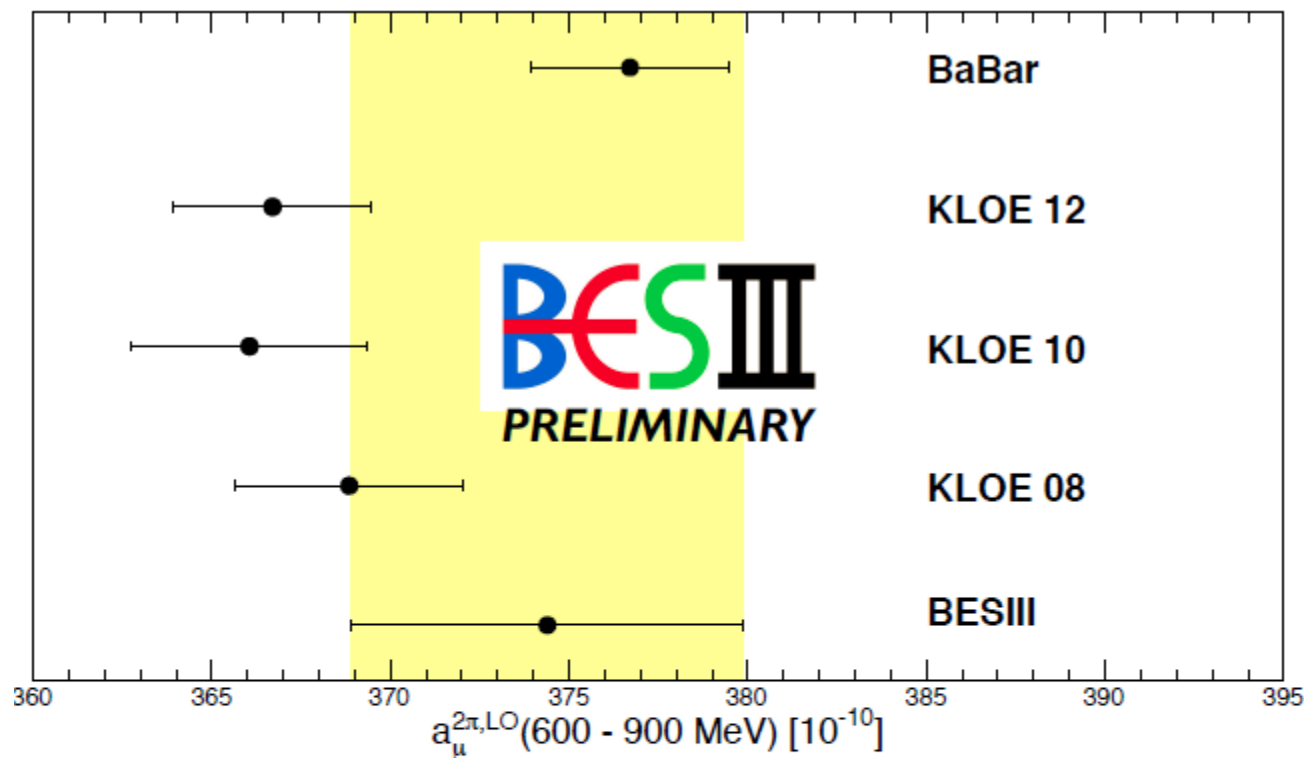


$$\chi^2 / \text{ndf} = 33.2 / 51$$

Form factor



Result for (g-2)



Experiment	$a_\mu^{2\pi, LO}(600 - 900 \text{ MeV}) [10^{-10}]$
BaBar	$376.7 \pm 2.0_{\text{stat}} \pm 1.9_{\text{sys}}$
KLOE 08	$368.9 \pm 0.4_{\text{stat}} \pm 2.3_{\text{sys,exp}} \pm 2.2_{\text{sys,theo}}$
KLOE 10	$366.1 \pm 0.9_{\text{stat}} \pm 2.3_{\text{sys,exp}} \pm 2.2_{\text{sys,theo}}$
KLOE 12	$366.7 \pm 1.2_{\text{stat}} \pm 2.4_{\text{sys,exp}} \pm 0.8_{\text{sys,theo}}$
BESIII (preliminary)	$374.4 \pm 2.6_{\text{stat}} \pm 4.9_{\text{sys}}$

Summary

◆proton pairs

- The effective form factors are measured with improved errors.
- The ratio $|G_E/G_M|$ were extracted at three energy points with uncertainty of 25% – 30% (statistic error dominant).
- The ratio $|G_E/G_M|$ are close to unity in 2.2 – 3.08 GeV.

◆pion pairs

- The cross section and form factor are measured with ISR return.
- The difference of Δa_μ between experiments and theory is confirmed.
- Systematic uncertainty ($\sim 1.3\%$) still dominant.

Prospect

Data samples between 2.0 – 3.08 GeV collected in 2015

E_{cm} (GeV)	E_{th} (GeV)	L_{Needed} (pb^{-1})	t_{beam} (days)	Purpose
2.0		≥ 8.95	14.6	Nucleon FFs
2.1		10.8	14.8	Nucleon FFs
2.15		2.7	2.29	$Y(2175)$
2.175		10(+)	8.5	$Y(2175)$
2.2		13	11	Nucleon FFs, $Y(2175)$
2.2324	2.2314	11	4	Hyp threshold ($\Lambda\Lambda$)
2.3094	2.3084	20	16	Nucleon & Hyp FFs Hyp Threshold ($\Sigma^0\bar{\Lambda}$)
2.3864	2.3853	20	8.7	Hyp Threshold ($\Sigma^0\Sigma^0$) Hyp FFs
2.3960	2.3949	≥ 64	27.8	Nucleon & Hyp FFs Hyp Threshold ($\Sigma^-\Sigma^+$)
2.5		0.4895	8h	R scan
2.6444	2.6434	65	18	Nucleon & Hyp FFs Hyp Threshold ($\Xi^-\Xi^+$)
2.7		0.5542	4.2h	R scan
2.8		0.6136	4h	R scan
2.9		100	18.5	Nucleon & Hyp FFs
2.95		15	2.8	$m_{p\bar{p}}$ step
2.981		15	2.8	η_c , $m_{p\bar{p}}$ step
3.0		15	2.8	$m_{p\bar{p}}$ step
3.02		15	2.8	$m_{p\bar{p}}$ step
3.08		120	13.2	Nucleon FFs (+30 pb^{-1})

Data : 19+2 energy points

Main goals

1. Cross section
2. Form factors
3. New states
4. R value

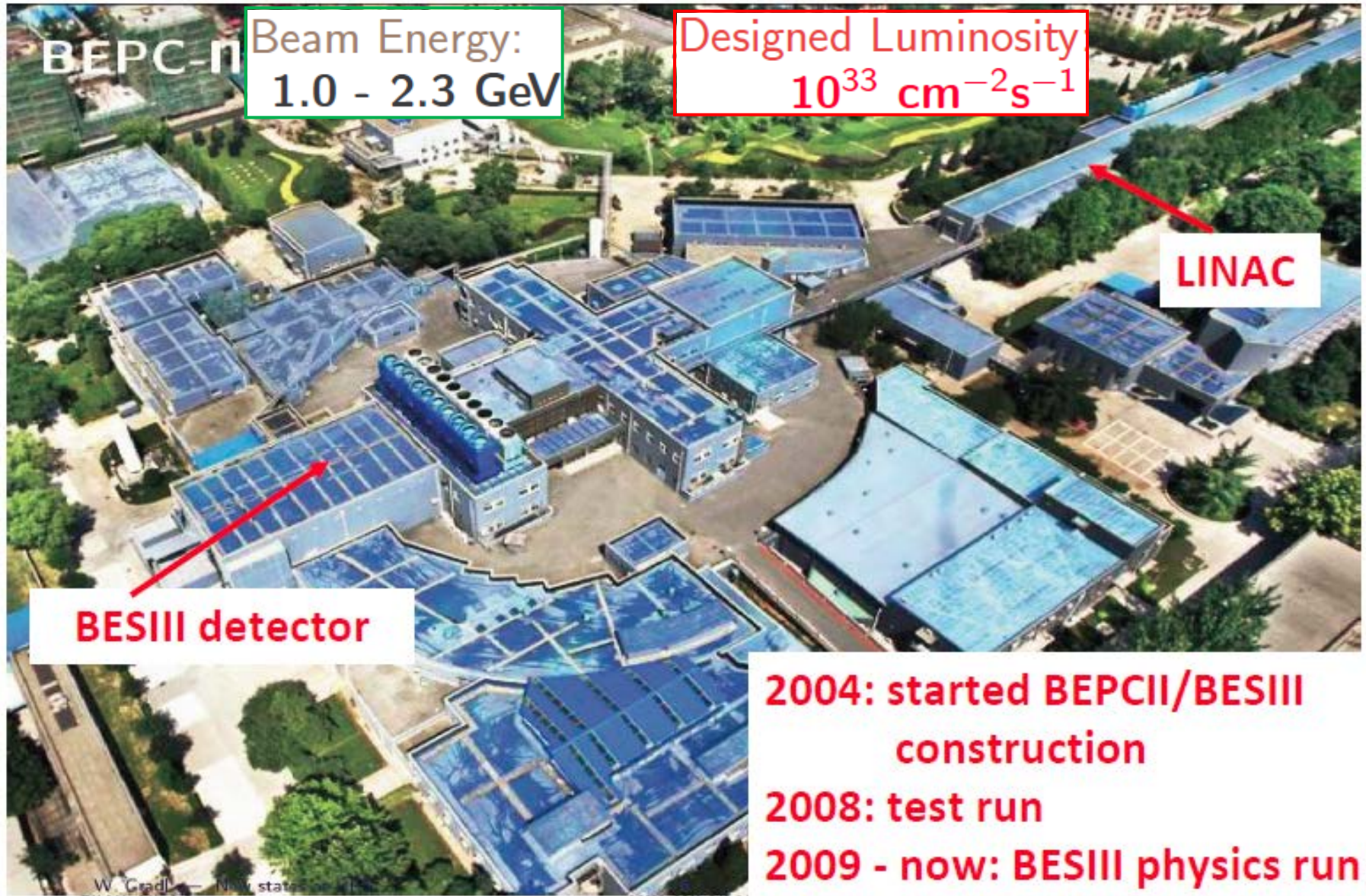
Prospect

- New data samples with larger statistics ($\sim 525\text{pb}^{-1}$) between 2.0–3.08 GeV at 21 energy points have collected in 2015.
- It may expect that more new results about handron production will be obtained at BESIII.

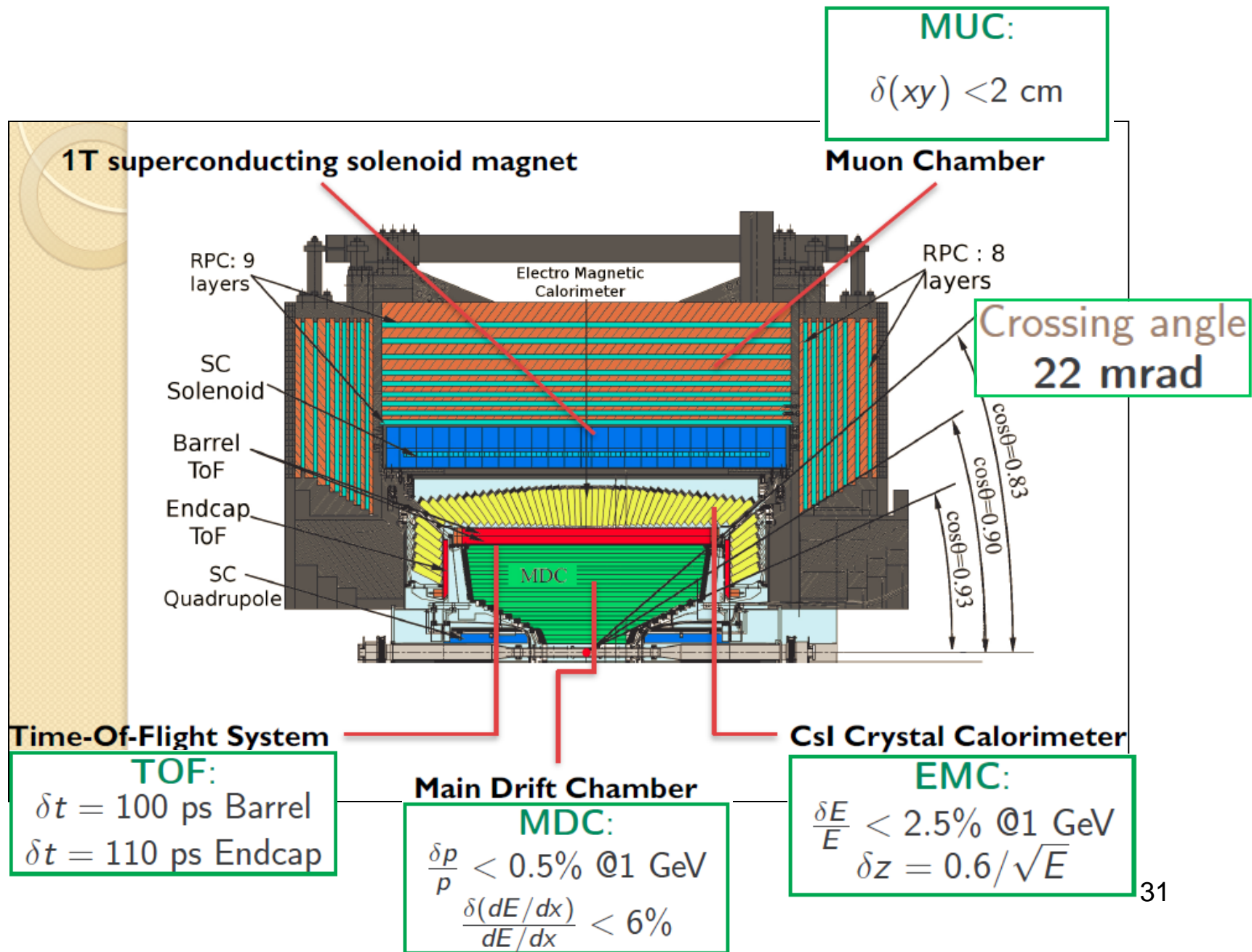
Thank you for your attention

Back up

Beijing Electron-Positron Collider II (BEPCII)



Beijing Spectrometer III (BESIII)

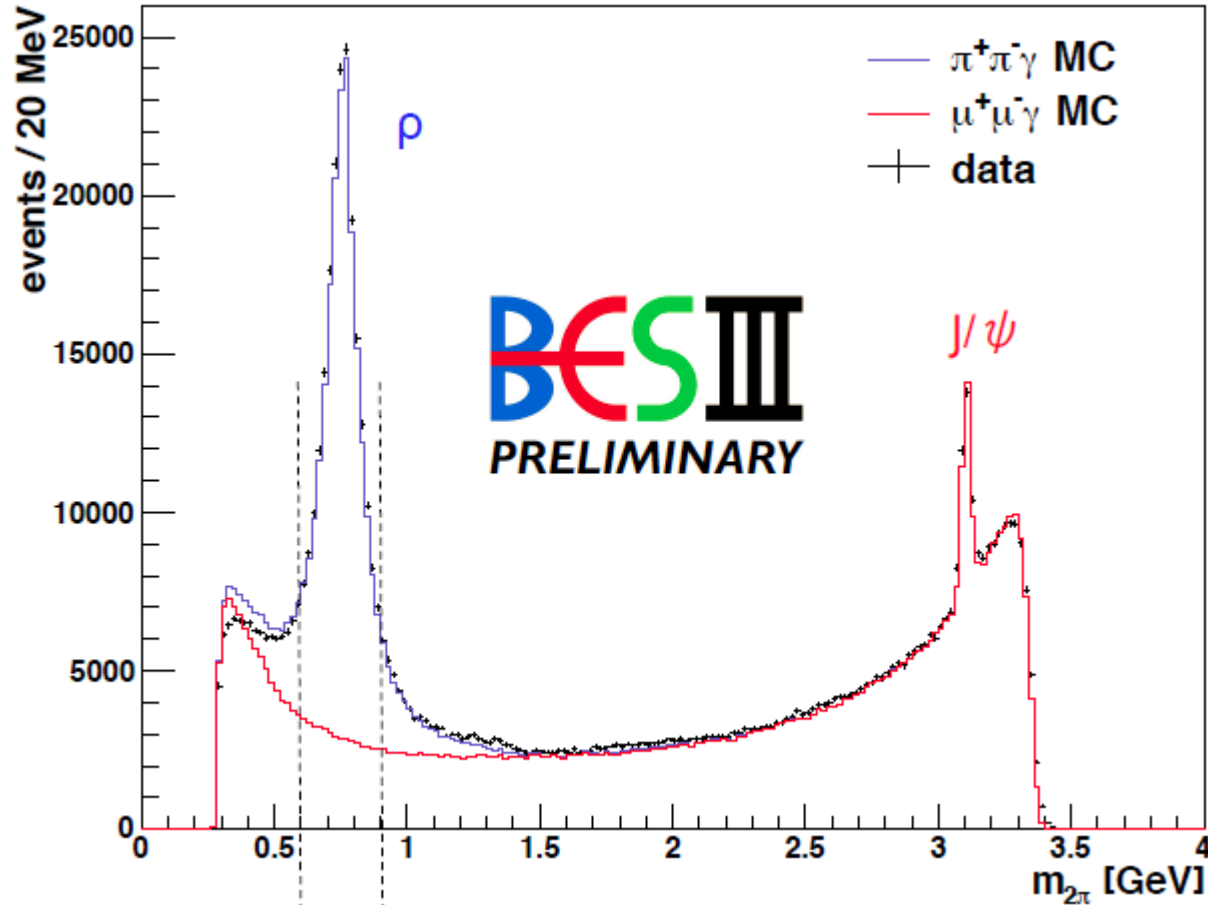


Overview of measurements of proton form factors

Some experiments measured proton form factors in scan and ISR return methods:

Process	Date	Experiment	q^2 (GeV ² /c ⁴)	q^2 point	Event	Precision
$e^+e^- \rightarrow p\bar{p}$	1972	FENICE/ADONE [17]	4.3	1	27	15%
	1979	DM1/ORSAY-DCI [18]	3.75-4.56	4	70	25.0%
	1983	DM2/ORSAY-DC1 [19]	4.0-5.0	6	100	19.6%
	1998	FENICE/ADONE [20]	3.6-5.9	5	76	19.3%
	2005	BES/BEPC [21]	4.0-9.4	10	80	21.2%
	2006	CLEO/ [22]	13.48	1	16	33.3%
$p^+p^- \rightarrow e^+e^-$	1976	PS135/CERN [24]	3.52	1	29	15.7%
	1994	PS170/CERN [25]	3.52-4.18	9	3667	6.1%
	1993	E760/Fermi [26]	8.9-13.0	3	29	33.8%
	1999	E835/Fermi [27]	8.84-18.4	6	144	10.3%
	2003	E835/Fermi [28]	11.63-18.22	4	66	21.1%
$e^+e^- \rightarrow \gamma + p\bar{p}$	2006	BaBar/SLAC-PEPII [30]	3.57-19.1	38	3261	9.8%
	2013	BaBar/SLAC-PEPII [31]	3.57-19.1	38	6866	6.7%
	2013	BaBar/SLAC-PEPII [32]	9.61-36.0	8	140	18.4%

ISR return analysis



- data: 2.9fb^{-1} @ $\psi(3773)$
- detect ISR γ
- BG: $\mu^+\mu^-\gamma$
- Initial publication

initial publication 600-900 MeV

Systematic uncertainties

source	uncertainty (%)
photon efficiency correction	0.2
pion tracking efficiency correction	0.3
pion ANN efficiency correction	0.2
pion e-PID efficiency correction	0.2
ANN	negl.
angular acceptance	0.1
muon background subtraction	0.06
non-muon background subtraction	0.03
unfolding	0.2
FSR correction δ_{FSR}	0.2
vacuum polarization correction δ_{vac}	0.2
radiator function	0.5
Luminosity \mathcal{L}	1.0 dominant
sum	1.3