Measurements of strong phase in $D^0 \to K\pi$ decay and y_{CP} via quantum-correlations at BESIII

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- Strong phase in $D^0 \rightarrow K\pi$ decay
- y_{CP} measurement

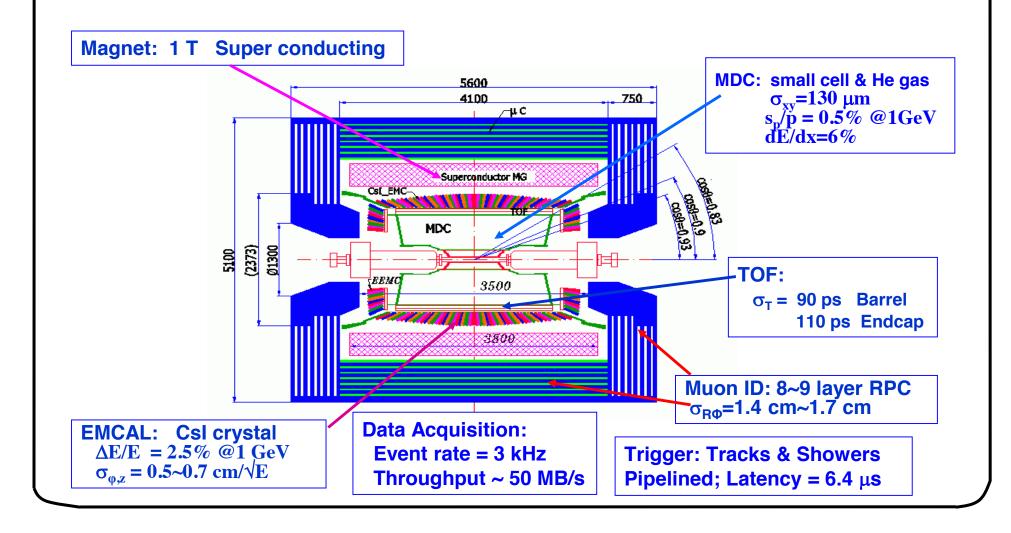
Beijing Electron Positron Collider (BEPC-II)

- A symmetric e⁺e⁻ collider, operating at Ecm ~ 2.0 ~4.6 GeV (Charm factory!).
- It's in Beijing: Easy access to the downtown area of Beijing with a nearby subway station!



BESIII detector

- A powerful general purpose detector.
- Excellent neutral and charged particle detection and identification with a large coverage.



Data samples we have

@ J/ψ peak : 1.2 B J/ψ decays and some scan in the vicinity of the peak.

@ $\psi(3686)$ peak : 0.5 B $\psi(3686)$ decays and some scan in the vicinity of the peak.

Above \overline{DD} threshold: 0.5/fb @ Ecm = 4.009 GeV, 1.9/fb @ Ecm = 4.26 GeV, 0.5/fb @ Ecm = 4.36 GeV, plus some scan samples as well.

The above samples have been producing very rich Physics results such as hadron spectroscopy of Charmonia (e.g., h_c/η_c) and of Charmonium-like states (X/Y/Z).

Today, I report recent results from BESIII based on a sample that was taken near DD threshold:

2.92/fb @Ecm = 3.773 GeV

Sample at $E_{cm} = 3.773 \text{ GeV}$

- The total integrated luminosity of 2.92 fb⁻¹ at this energy point is the largest in the world to date.
- In the selected hadronic events (multiple reconstructed charged/ neutral hadrons or tracks), they are dominated by;

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e^+e^- \rightarrow \gamma^* \rightarrow \psi(3770) and e^+e^- \rightarrow \gamma^* \rightarrow (q\bar{q}) light hadrons
in which
 \sigma(e^+e^- \rightarrow \psi(3770) \rightarrow hadrons)/\sigma(e^+e^- \rightarrow NR \rightarrow hadrons) \sim 1/2.
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- Once $\psi(3770)$ is produced, it predominantly decays into a DD pair. For instance, we have ~21 M D⁰ (or \overline{D}^0) decays in this sample.
 - Relatively clean event environment.
 - When the two D mesons are reconstructed, the sample becomes almost background free.

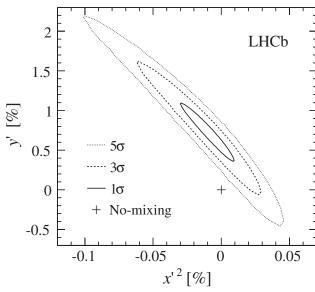
Things can be done with the sample taken at or around $E_{cm} = 3.773 \text{ GeV}$

- There are many interesting possible topics to study in D (weak) decays based on our sample, such as;
 - pure leptonic decays (e.g., extraction of $|V_{cd}|$ and/or its decay constant, f_D).
 - Semi-leptonic decays (e.g., extraction of their form factors, and then compare them vs B meson case).
 - With the largest sample of D mesons taken at the near threshold, one should look for rare/forbidden decays (e.g., FCNC, LNV, LFV).
 - or even $\psi(3770)$ itself such as $\psi(3770) \rightarrow$ non-DD final states.
- But today, I report our attempt to measure some of the parameters of DD mixing using the unique characteristics of our $\psi(3770)$ data set taken at $E_{cm} = 3.773$ GeV.

Introduction

- DD mixing is highly suppressed by the GIM mechanism and by the CKM matrix elements within the Standard Model.
- Observation of DD mixing, first seen by the B factories (HFAG: arXiv 1207.1158) and now observed by LHCb: PRL110, 101802 (2013).
- Improving the constraints on the charm mixing parameter is important for testing the SM, such as long distance effects.
- DD mixing is conventionally described by two parameters:

$$x = 2(M_1-M_2)/(\Gamma_1+\Gamma_2), y = (\Gamma_1-\Gamma_2)/(\Gamma_1+\Gamma_2),$$



where $M_{1,2}$ and $\Gamma_{1,2}$ are the masses and widths of the neutral D meson mass eigenstates. (Flavor eigenstates, $D^0/\overline{D^0}$, are not the same as mass eigenstates, D_1/D_2)

Or
$$x' = x \cdot \cos \delta_{K\pi} + y \cdot \sin \delta_{K\pi}$$
, $y' = y \cdot \cos \delta_{K\pi} - x \cdot \sin \delta_{K\pi}$.

- $\delta_{K\pi}$ is the strong phase difference between the doubly Cabibbo suppressed (DCS) decay, $\overline{D^0} \rightarrow K^-\pi^+$ and the Cabibbo favored (CF) decay, $D^0 \rightarrow K^-\pi^+$ or $\langle K^-\pi^+|\overline{D^0}\rangle/\langle K^-\pi^+|D^0\rangle = -r \cdot e^{-i\delta}$. So one can connect (x,y) with (x',y') via $\delta_{K\pi}$.
- In this talk, I present preliminary results on $\delta_{K\pi}$ and y using the quantum correlation between the produced D⁰ and D⁰ pair in data taken at BESIII.

The decay rate of a correlated state

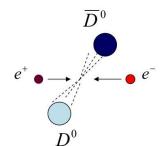
For physical process producing D⁰D

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such as

$$e^+e^- \rightarrow \gamma^* \rightarrow \psi(3770) \rightarrow D^0\overline{D}^0$$
,



the $D^0\overline{D^0}$ pair are in a quantum-correlated state.

The quantum number of $\psi(3770)$ is $J^{PC} = 1^{-1}$.

Thus, the $D^0\overline{D^0}$ pair in this process has C = -.

For a correlated state with C = -, the two D mesons are anti-symmetric in the limit of CP invariance:

$$\psi_{-} = \frac{1}{\sqrt{2}} (\left| D^{0} \right\rangle \left| \overline{D}^{0} \right\rangle - \left| \overline{D}^{0} \right\rangle \left| D^{0} \right\rangle)$$

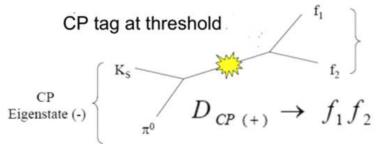
- The two produced neutral mesons must have opposite CP (i.e., see Goldhaber and Rosner, PRD15, 1254 (1977). That is;
 - ▶ Final states of (CP+, CP+) or (CP-, CP-) are forbidden.
 - ▶ Final states of (CP+, CP-) are maximally enhanced (doubled).
 - ▶ Final states of CP± against inclusive states (Single tag or ST) are not affected.
 - \blacktriangleright Final states of (K- π +, CP±) are affected due to the interference between CF and DCS $(\delta_{K\pi}).$

Extracting $\delta_{K\pi}$

▶ Neglecting higher orders in the mixing parameters (e.g., y²), one can arrive at the following relation:

$$2 \cdot \mathbf{r} \cdot \mathbf{cos} \delta_{K\pi} + \mathbf{y} = (1 + R_{WS}) \cdot A_{CP \to K\pi},$$
where $R_{WS} \equiv \Gamma(\overline{D}^0 \to K^-\pi^+) / \Gamma(D^0 \to K^-\pi^+)$ and
$$A_{CP \to K\pi} \equiv [B(D_2 \to K^-\pi^+) - B(D_1 \to K^-\pi^+)] / B(D_2 \to K^-\pi^+) + B(D_1 \to K^-\pi^+)].$$

• We can extract $A_{CP\to K\pi}$ by tagging one D (tag side) with exclusive CP-eigenstates which then defines the eigenvalue of the other D ($A_{CP\pm} \equiv \langle K^-\pi^+|D^{1,2}\rangle$).



- ▶ Then, with the knowledge of r, y, and R_{WS} from the 3rd parties (HFAG2013 and PDG), we could derive $\cos \delta_{K\pi}$ in the end.
- ▶ The rest of the analysis becomes measurements of $B(D_{CP\pm} \to K^-\pi^+)$ while simultaneously reconstructing the D_{CP} on the tag side.

Measuring $B(D_{CP\pm} \rightarrow K^-\pi^+)$

Double-Tag technique:

$$B(D_{CP\pm} \to K\pi) = [B(D_{CP\mp} \to CP^{\mp} \text{ states}) \times B(D_{CP\pm} \to K\pi)]/B(D_{CP\mp} \to CP^{\mp} \text{ states})$$

= $(n_{K\pi,CP\mp}/n_{CP\mp}) \cdot (\epsilon_{CP\mp}/\epsilon_{K\pi,CP\mp})$,
where $n_{K\pi,CP\mp}$ are yields of " $K\pi$ " when CP states are

simultaneously reconstructed on the tag side

n_{CP∓} are yields of CP states (independent of how the other D decays)

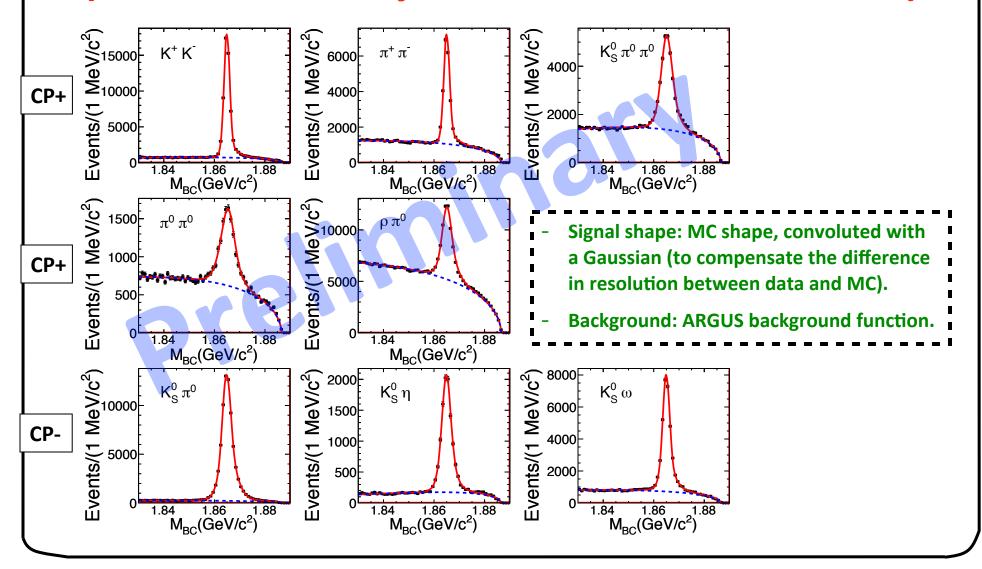
 ϵ_{CP} and $\epsilon_{K\pi,CP}$ are the corresponding reconstruction efficiencies.

- "Yields" are extracted from M_{bc} distributions : $M_{BC} = \sqrt{E_{beam}^2 \vec{p}_D^2}$
- CP states on Tag side (8 modes): $CP+ K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$ $CP- K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

where we reconstruct $K_S \rightarrow \pi^+\pi^-$, $\pi^0/\eta \rightarrow \gamma\gamma$, $\omega \rightarrow \pi^+\pi^-\pi^0$, $\rho \rightarrow \pi^+\pi^-$.

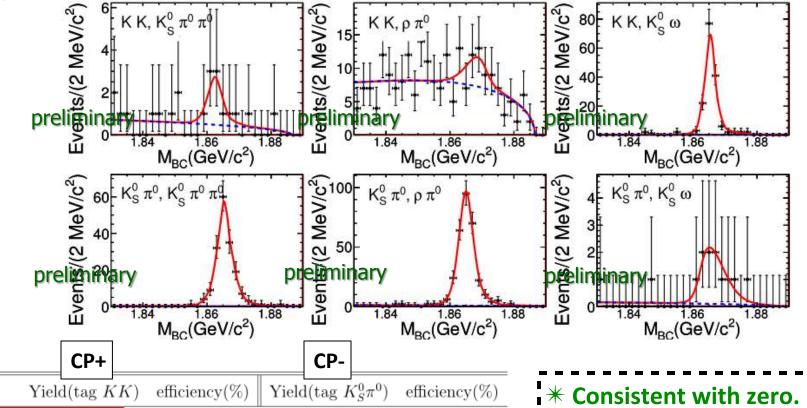
• Notice that most of systematics on the tag side get canceled in $B(D_{CP\pm}\to K\pi)$. The remaining systematics (reconstruction/simulation) of $K\pi$ are also canceled in the determination of $A_{CP\to K\pi}$.

Yields of CP states (n_{CP∓}) (reconstruct only one of the two neutral D)



Can also check "CP purity"

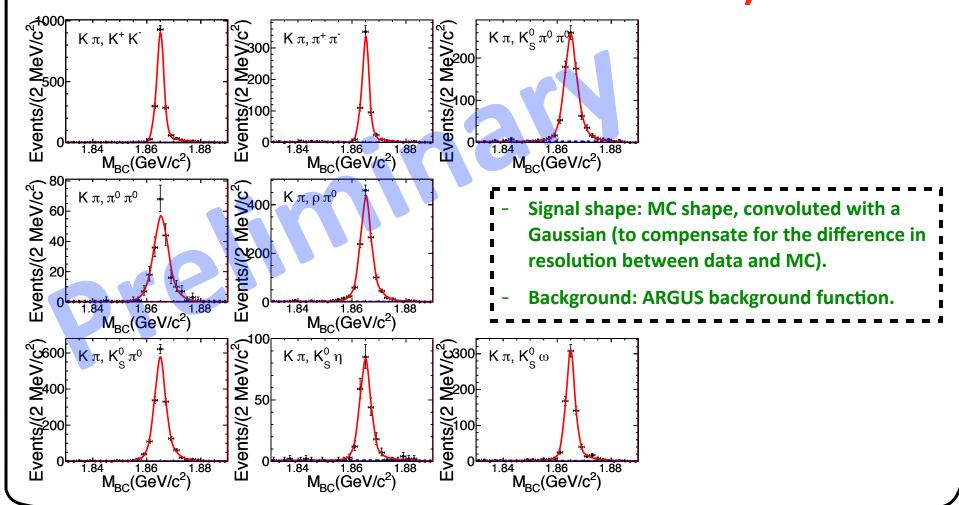
When D^0 and \overline{D}^0 are reconstructed, final states with the same CP should yield zero events.



ſ		Mode	Yield(tag KK	\mathcal{K}) efficiency(%)	Yield(tag $K_S^0 \pi^0$)	efficiency($\%$)
	CP+	$K^0_S\pi^0\pi^0$	$8 \pm 3(*)$	11.80 ± 0.11	171 ± 14	7.20 ± 0.09
	CP+	$\rho\pi^0$	$13 \pm 8(*)$	24.44 ± 0.16	299 ± 19	15.87 ± 0.16
	CP-	$K_S^0 \omega$	158 ± 13	11.02 ± 0.11	7 ± 3(*)	6.77 ± 0.08

- * Consider as one of the systematics.

Yields of Kπ in double tags $(n_{Kπ,CP})$ (reconstruct CP-final state from one D decay, with " $K\pi$ " from the other D)



Preliminary fit results

Mode(CP)	ST Yield	$\operatorname{Efficiency}(\%)$
K^+K^-	$56156 \pm 261 \pm 61$	62.99 ± 0.26
$\pi^+\pi^-$	$20222 \pm 187 \pm 38$	65.58 ± 0.26
$K^0_S\pi^0\pi^0$	$25156 \pm 235 \pm 81$	16.46 ± 0.07
$\pi^0\pi^0$	$7610\pm156\pm56$	42.77 ± 0.21
$\rho\pi^0$	$41117 \pm 354 \pm 68$	36.22 ± 0.21
$K_S^0\pi^0$	$72710 \pm 291 \pm 34$	41.95 ± 0.21
$K^0_S\eta$	$10046 \pm 118 \pm 27$	35.46 ± 0.20
$K^0_S\omega$	$31422 \pm 215 \pm 49$	17.88 ± 0.10

Mode	DT Yield	$\operatorname{efficiency}(\%)$
$K^{\pm}\pi^{\mp}, K^{+}K^{-}$	$1669 \pm 42 \pm 4$	42.65 ± 0.21
$K^{\pm}\pi^{\mp},\pi^{+}\pi^{-}$	$608 \pm 25 \pm 3$	44.32 ± 0.21
$K^\pm\pi^\mp, K^0_S\pi^0\pi^0$	$800 \pm 30 \pm 4$	12.68 ± 0.13
$K^{\pm}\pi^{\mp},\pi^0\pi^0$	$212\pm15\pm0$	29.75 ± 0.18
$K^{\pm}\pi^{\mp},\rho\pi^{0}$	$1240\pm36\pm1$	25.44 ± 0.16
$K^{\pm}\pi^{\mp}, K^0_S\pi^0$	$1688\pm42\pm4$	29.06 ± 0.17
$K^{\pm}\pi^{\mp}, K^0_S\eta$	$231\pm16\pm1$	24.76 ± 0.16
$K^{\pm}\pi^{\mp}, K^0_S\omega$	$725 \pm 28 \pm 1$	12.47 ± 0.06

- These yields allow us to obtain $B(D_{CP\pm} \to K^-\pi^+)$ which then provides $A_{CP\to K\pi}$.
- $A_{CP\to K\pi}$ = (12.77±1.31(stat.)^{+0.33}_{-0.31}(syst.))%.

Preliminary result on $\delta_{K\pi}$

- We have measured $A_{CP\to K\pi} = (12.77\pm1.31(\text{stat.})^{+0.33}_{-0.31}(\text{syst.}))\%$.
- Using the relation, $2 \cdot r \cdot \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot A_{CP \to K\pi}$, and with external inputs from HFAG2013 and PDG (R_D = 3.47±0.06%, y=6.6±0.9%, R_{WS} = 3.80±0.05%), we obtain

 $\cos \delta_{K\pi} = 1.03\pm 0.12 (\text{stat.})\pm 0.04 (\text{syst.})\pm 0.01 (\text{external}).$

 Our result is consistent with and more precise than the recent CLEO result (PRD86, 112001 (2012)):

$$\cos \delta_{K\pi} = 1.15^{+0.19}_{-0.17} (\text{stat.})^{+0.00}_{-0.08} (\text{syst.}).$$

Determination of the mixing parameter, y_{CP}

y_{CP} is defined as;

 $2 \cdot y_{CP} = (|q/p|+|p/q|) \cdot y \cdot \cos \phi \cdot (|q/p|-|p/q|) \cdot x \cdot \sin \phi$, where p and q are mixing parameters, and $\phi = \arg(q/p)$ is the weak phase difference of the mixing amplitudes.

Notice: for no CPV case, $p = q = 1/\sqrt{2}$ and $y_{CP} \equiv y$.

 $|D_1\rangle = p|D^0\rangle + q|\overline{D}^0\rangle$

 $|D_2\rangle = p|D^0\rangle - q|\overline{D}^0\rangle$

For D decays into any CP-eigenstate, its decay rate can be described as;

$$R(D^0/\overline{D^0} \rightarrow CP^{\pm}) \propto |A_{CP\pm}|^2 \cdot (1 \mp y_{CP}).$$

- When one D decays into a CP-eigenstate, while the other D decays semi-leptonically, the decay rate can be given by;

$$R(D^0/\overline{D}^0 \rightarrow CP^{\pm}, \text{ and } \overline{D}^0/D^0 \rightarrow \text{semi-lep}) \propto |A_1|^2 \cdot |A_{CP^{\pm}}|^2$$
.

- Semileptonic decay width does not depend on the CP of its parent D.
- Yet, the total width of its parent D depends on CP.
- Result: semileptonic BF of $D_{1,2}$ gets modified by a factor of $1\pm y_{CP}$.
- Combining the above two, and neglecting terms with y2 (or higher), one can arrive at

$$y_{CP} = \frac{1}{4} \left(\frac{R_{l;CP+} R_{CP-}}{R_{l:CP-} R_{CP+}} - \frac{R_{l;CP-} R_{CP+}}{R_{l:CP+} R_{CP-}} \right)$$

Extracting y_{CP} in our experiment

The expression for y_{CP} can be written as;

$$y_{CP} = \frac{1}{4} \left[\frac{\tilde{B}_+}{\tilde{B}_-} - \frac{\tilde{B}_-}{\tilde{B}_+} \right]$$

where \tilde{B}_{\pm} is the branching fraction, averaged over different CP tag modes, α , that is obtained by minimizing

$$\chi^2 = \sum_{\alpha} \frac{(\tilde{B}_{\pm} - B_{\pm}^{\alpha})^2}{(\sigma_{\pm}^{\alpha})^2}$$

- All branching fractions are obtained in a similar way, the double-tag method.
- When the semileptonic decays are reconstructed, however, we use Umiss distributions to obtain their yields, instead of Mbc,

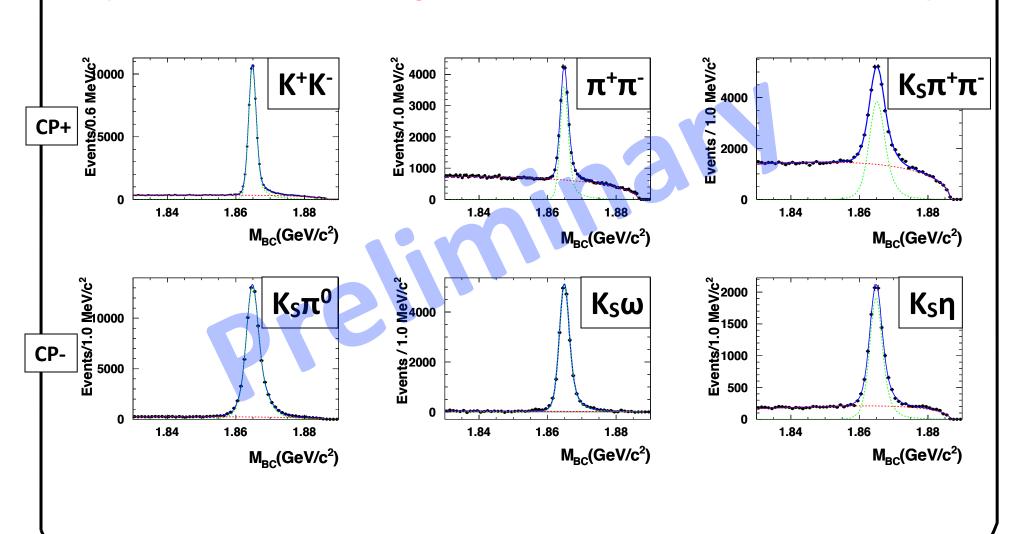
$$U_{
m miss} \equiv E_{
m miss} - |\vec{p}_{
m miss}|$$
 ,

which peaks ~ 0 if only missing particle is neutrino.

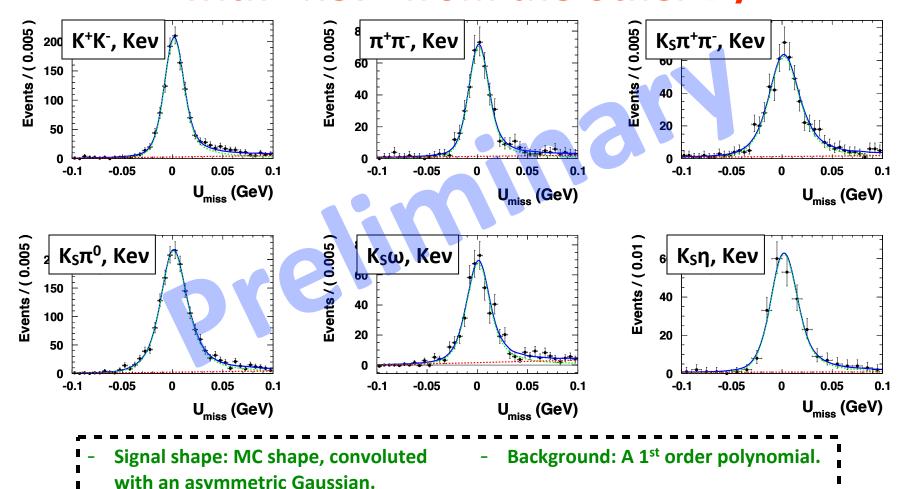
Tag modes:

Type	Modes
CP^+	$K^+K^-, \pi^+\pi^-, K_S\pi^0\pi^0$
CP^-	$K_S^0 \pi^0, K_S^0 \omega, K_S^0 \eta$
l^{\pm}	$Ke\nu, K\mu\nu$

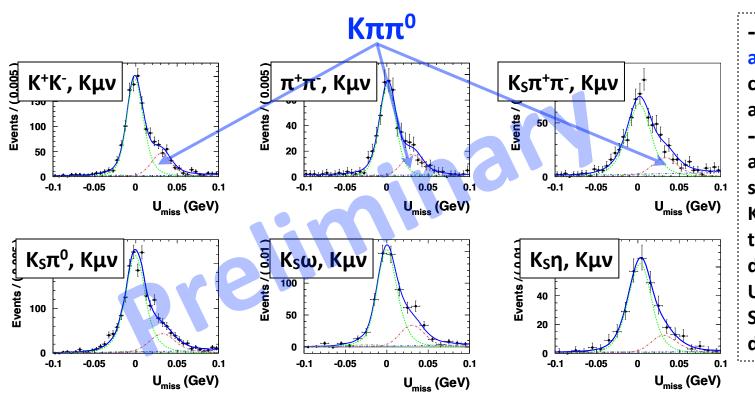
Yields of CP states $(n_{CP} \mp)$ (reconstruct only one of the two neutral D)



Yields of Kev in double tags $(n_{Kev,CP} \mp)$ (reconstruct CP-final states from one D decay, with "Kev" from the other D)



Yields of Kµv in double tags $(n_{Kµv,CP} \mp)$ (reconstruct CP-final states from one D decay, with "Kµv" from the other D)



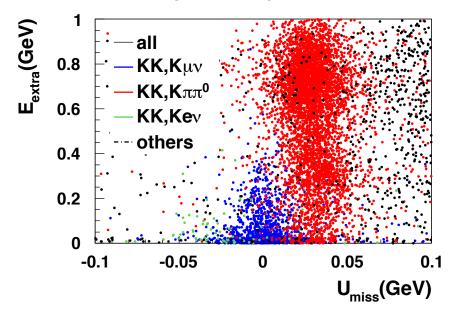
- $K\pi\pi^0$ shapes and sizes are fixed based on control samples of actual data.
- The control samples are obtained by the same CP states and $K\pi\pi^0$, while ignoring the two photons from π^0 decays to calculate Umiss.

See the next slide for detail.

- Signal shape: MC shape, convoluted with an asymmetric Gaussian.
- Background: A 1st order polynomial. Kππ⁰ (dominant).

Fixing the Kππ⁰ shape

- Obtain E_{extra} ≡ Sum of the all un-used energies deposited in EM calorimeter.
- E_{extra} tends to be larger if it is $K\pi\pi^0$ due to the ignored extra photons from π^0 decay and is small if it is $K\mu\nu$.
- We actually do require E_{extra} <0.2 GeV to select $K\mu\nu$ signal candidates.



Fix shape

- Fit to U_{miss} in $E_{extra}>0.5$ GeV where $K\mu\nu$ peak is suppressed.
- The fitted shape
 ■ MC shape,
 convoluted with a Gaussian.

Fix size

 $(K\pi\pi^0 \text{ yields in data in } E_{\text{extra}} < 0.2 \text{ GeV}) = R \times (K\pi\pi^0 \text{ yields in data in } E_{\text{extra}} > 0.5 \text{ GeV}),$ where R = $(K\pi\pi^0 \text{ yields in MC in } E_{\text{extra}} < 0.2 \text{ GeV})/(K\pi\pi^0 \text{ yields in MC in } E_{\text{extra}} > 0.5 \text{ GeV}).$

Preliminary results

Fitted yields for each mode:

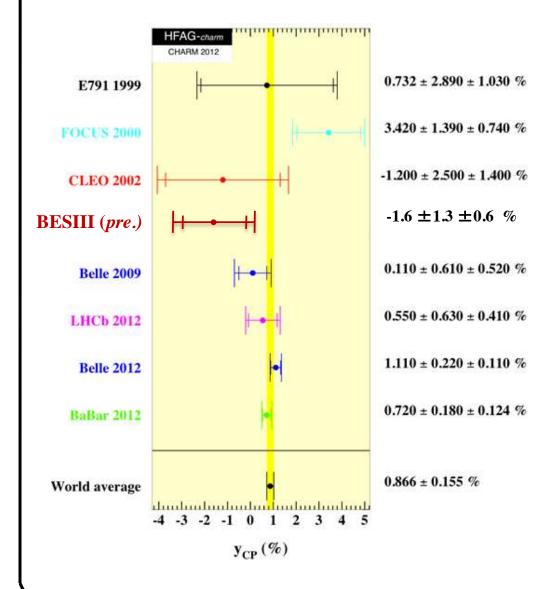
Modes	N_{tag}	$N_{tag,Ke\nu}$	$N_{tag,K\mu\nu}$
K^+K^-	54307 ± 252	1216 ± 40	1093 ± 37
$\pi^+\pi^-$	19996 ± 177	427 ± 23	400 ± 23
$K_S^0\pi^0\pi^0$	19996 ± 177 24369 ± 231	560 ± 28	558 ± 28
$K^0_S\pi^0$	71419 ± 286	1699 ± 47	1475 ± 43
$K^0_S\omega$	21249 ± 157	473 ± 25	501 ± 26
$K^0_S\eta$	9843 ± 117	242 ± 17	237 ± 18

After correcting for efficiencies (branching fractions),
 we arrive at

$$y_{CP} = [-1.6\pm1.3(stat.)\pm0.6(syst.)]\%$$
.

- The result is statistically limited.
- The systematic uncertainty mainly comes from fitting procedures.

Comparison with other measurements



- Our result is consistent with the world average (HFAG2013; this preliminary result is not included in the average).
- Also consistent with the latest result from CLEO-c (PRD86, 112001 (2012)); $y_{CP} = (4.2 \pm 2.0 \pm 1.0)\%.$ (not listed in the figure).

Summary

- Quantum-correlated $D^0\overline{D^0}$ in e^+e^- annihilations near threshold: Unique way to measure the Charm mixing parameters.
- Most precise measurement of strong phase difference in D⁰→ Kπ.
 Will improve the determination of mixing parameters, x and y.
- Measurement of y_{CP}:
 Statistically limited, consistent with the world average.
- Will collect larger "open-charm" data samples in years to come: Expect many interesting results.